## The Far-infrared Absorption Intensities and the Dipole Moments of Acetone and Dimethyl Sulfoxide in Solutions

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(Received November 12, 1980)

**Synopsis.** The effective dipole moments of acetone and dimethyl sulfoxide in nonpolar solutions were obtained from the far-infrared absorption intensities on the basis of an extended Onsager model with an eccentric point dipole.

Dipolar molecules in the liquid phase have absorptions in the far-infrared region<sup>1-5)</sup> due to the rotational motion of the molecules and the temporary dipole moments induced by collision. However, the collision-induced absorption is generally much weaker than the dipolar absorption.<sup>6)</sup> If the far-infrared absorption is attributed solely to the rotational motion of the molecule, the effective dipole moment can be obtained using Gordon's sum rule7) after correcting for the internal-field effect.<sup>8,9)</sup> In a previous study of CH3I, CHCl3, CH2Cl2, and CH3CN in solutions,5) the far-infrared absorption intensities were explained successfully by taking into account the internal-field effect and the internal moment<sup>10)</sup> based upon Onsager's model. In the present study, far-infrared absorption intensities were measured for acetone and dimethyl sulfoxide (DMSO) in dilute C<sub>6</sub>H<sub>6</sub>, CCl<sub>4</sub>, C<sub>2</sub>Cl<sub>4</sub>, and n-C<sub>6</sub>H<sub>14</sub> solutions. The observed intensities, however, cannot be interpreted by the same model as was employed in the previous study. Therefore, the model for the reaction field has been extended to a model with an eccentric dipole-location.

## Experimental

The far-infrared spectra were measured at room temperature by means of an apparatus described previously.<sup>5)</sup> Solutions were prepared from spectroscopic-grade reagents except for the deuterated compounds, which were already more than 99.6% pure when obtained from CEA and Merck. The concentration range was 0.06—0.17 M.

## Results and Discussion

The absorption coefficients,  $\sigma(v)$ , of the solutes in nonpolar solvents are given by:

$$\sigma(\nu) = (1/\rho l) \ln(T_0/T)_{\nu}, \tag{1}$$

where  $\rho$  is the concentration (molecules cm<sup>-3</sup>); l, the sample thickness (cm), and  $T_0$  and T, the transmittances of the solvent and the solution respectively. The observed results are shown in Fig. 1, where the fine broken lines indicate the spectra profiles assumed in order to obtain the intensities,  $A = \int \sigma(v) dv$ . The value of A for each solution was determined by measurements at four concentrations. The results obeyed Beer's law. The A values were estimated, from the fluctuation of the four measurements, to be within  $\pm 3\%$ . The systematic errors are due mainly to uncertainties in the assumed curves. The area of the assumed portion is 3-4% of the total area. Thus,

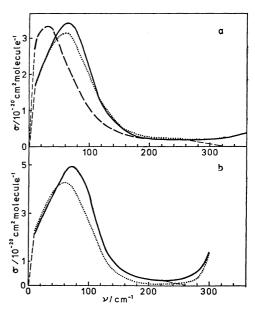


Fig. 1. a) Far-infrared absorption bands of  $(CH_3)_2CO$  dissolved in  $CCl_4(---)$ , in  $C_6H_6(----)$ , and n- $C_6H_{14}$  (----). b) Far-infrared absorption bands of  $(CH_3)_2$ -SO dissolved in  $CCl_4(----)$ , and in  $C_6H_6(----)$ .

the total experimental errors in A were estimated to be  $\pm 5\%$  at most.

The intensities, as corrected for the internal field effect,  $A_e$ , are given as:<sup>8,9)</sup>

$$A_{c} = xA, \quad x = n_{s}\{[(n/n_{s})^{2} + 2]/(n^{2} + 2)\}^{2},$$
 (2)

where n and  $n_{\rm s}$  are the refractive indices of the solute and the solvent respectively. For  ${\rm C_{2v}}$  symmetric molecules, Gordon's sum rule is expressed by:7)

$$A_{c} = (\pi \mu^{2}/3c^{2})(1/I_{x} + 1/I_{y}), \qquad (3)$$

where c is the velocity of light;  $\mu$ , the effective dipole moment taken along the z axis, and  $I_x$  and  $I_y$ , the moments of inertia about the x and y axes respectively. The  $\mu$  values,  $\mu_I$ , obtained from Eq. 3 are shown in the fourth column of Table 1, together with the values of the moments of inertia and the permanent dipole moments in the gas phase,  $\mu_0$ . The  $\mu_I$  values for the H-compounds are in good agreement with those for the D-compounds, which have different moments of inertia. Furthermore, the  $\mu_I$  values are about 10-30% larger than the  $\mu_0$  values for all the solutions.

In Onsager's model, the internal moment,  $\mu_1^*$ , is expressed as:<sup>10,11)</sup>

$$\mu^*_{\mathbf{I}} = \mu_0(n^2 + 2)(2\varepsilon + 1)/3(2\varepsilon + n^2), \tag{4}$$

where  $\varepsilon$  is the dielectric constant of the uniform medium and can be replaced by  $n_s^2$  to a good approximation. The  $\mu_1^*$  values calculated from  $\mu_0$  are listed in the fifth column of Table 1. However, the  $\mu_1$ 

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Solute	Solvent	$\boldsymbol{A}$	$\mu_{\mathrm{I}}$	$\mu^*_{\mathbf{I}}$	$\mu_{ ext{II}}$	$\mu *_{\text{II}}$	$\mu_0$	$I^{ m b)}$
	Solvent	$10^{-19} \text{ cm mol}^{-1}$	D			$10^{-40}  \mathrm{g \ cm^2}$		
$(\mathrm{CH_3})_2\mathrm{CO}$	$C_6H_6$	34.6	3.65	3.26	3.48	3.42	2.93c)	$I_{\rm x} = 82.56, I_{\rm y} = 170.9$
	$CCl_4$	35.8	$3.7_2$	$3.2_{4}$	$3.5_{6}$	$3.3_{8}$		
	$C_2Cl_4$	33.1	$3.5_{7}$	$3.2_{6}$	$3.4_{0}$	$3.4_2$		
	$n$ - $\mathrm{C_6H_{14}}$	29.5	$3.4_{1}$	3.19	$3.2_{8}$	$3.3_{1}$		
$(\mathrm{CD_3})_2\mathrm{CO}$	$CCl_4$	30.0	$3.7_{5}$	$3.2_{4}$	$3.5_{8}$	$3.3_{8}$		$I_{\rm x} = 99.09, I_{\rm y} = 209.2$
$(CH_3)_2SO$	$C_6H_6$	40.6	$4.4_{3}$	$4.5_{5}$	$4.1_{6}$	$4.8_{5}$	$3.96^{\circ}$	$I_{\rm x} = 119.3, I_{\rm y} = 198.9$
	$CCl_4$	51.1	$5.0_{0}$	$4.5_{1}$	$4.7_{1}$	$4.7_{9}$		
$(\mathrm{CD_3})_2\mathrm{SO}$	$\mathbf{C_6H_6}$	35.6	$4.5_{1}$	$4.5_{5}$	$4.2_{3}$	$4.8_{5}$		$I_{\rm x} = 139.2, I_{\rm y} = 241.0$
	$CCl_4$	43.4	$5.0_1$	$4.5_{1}$	$4.7_{2}$	$4.7_{9}$		

a) I: The simple Onsager model; II: The eccentric dipole model. b) Calculated from the rotational constants taken from Ref. 12. c) Ref. 13.

values are larger by about 10% or more than the  $\mu_1^*$  values except for that of DMSO in the  $C_6H_6$  solutions. Onsager's model was extended to a model with an ellipsoidal cavity and an eccentric point dipole. It turned out that, in nonpolar solvents, the magnitude of the reaction-field effect was almost independent of the cavity shape, but was significantly dependent on the position of the dipole in the cavity. For a molecule with an eccentric point dipole in a spherical cavity, the internal-field correction factor, x, and the internal moment,  $\mu^*$ , are given by: II)

$$x = n_{\rm s}[3\varepsilon/(2\varepsilon+1)(1-f\cdot\alpha)]^{-2},\tag{5}$$

$$\mu^* = \mu_0/(1-f\cdot\alpha),\tag{6}$$

where:

$$f = (1/a^3) \sum_{m=1}^{\infty} [m^2(m+1)(\varepsilon-1)/(m+m\varepsilon+\varepsilon)](s/a)^{2m-2},$$
 (7)

and where  $\alpha$  is the average polarizability of the molecule, a is the radius of the cavity, and s is the distance from the center of the cavity to the point dipole. The parameter, s/a, is a measure of the eccentricity of the position of the dipole.  $\alpha$  and a are related in a good approximation by:<sup>10</sup>

$$\alpha = a^3(n^2 - 1)/(n^2 + 2). \tag{8}$$

If s=0, Eqs. 5 and 6 reduce to Eqs. 2 and 4. The  $\mu$  and  $\mu^*$  values thus calculated with s/a=0.3,  $\mu_{\rm II}$  and  $\mu_{\rm II}^*$ , are shown in Table 1. There is no other means to confirm the propriety of the s/a value. However, a good agreement between  $\mu_{\rm II}$  and  $\mu_{\rm II}^*$  is obtained except for the  $C_6H_6$  solutions of DMSO. For acetone, the internal moments are the least in the hexane solutions and almost the same in the other solutions, reflecting the dielectric constants of the solvents. Unlike as in the results for acetone, the  $\mu_{\rm II}$  value in the  $C_6H_6$  solutions of DMSO is distinctly smaller not only than that in the CCl<sub>4</sub> solutions, but

also than the  $\mu_{11}^{**}$  value. There seems to exist a short-range ordering of  $C_6H_6$  molecules around a DMSO molecule, such as the alignment of benzene rings perpendicular to the direction of the dipole moment of DMSO. The reaction field becomes weak because the axial polarizability of benzene molecules is smaller than the average polarizability, and so a  $\mu_{11}$  value smaller than the  $\mu_{11}^{**}$  value is obtained.

The authors wish to thank Dr. Shun-ichi Ikawa for his valuable suggestions and discussions.

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